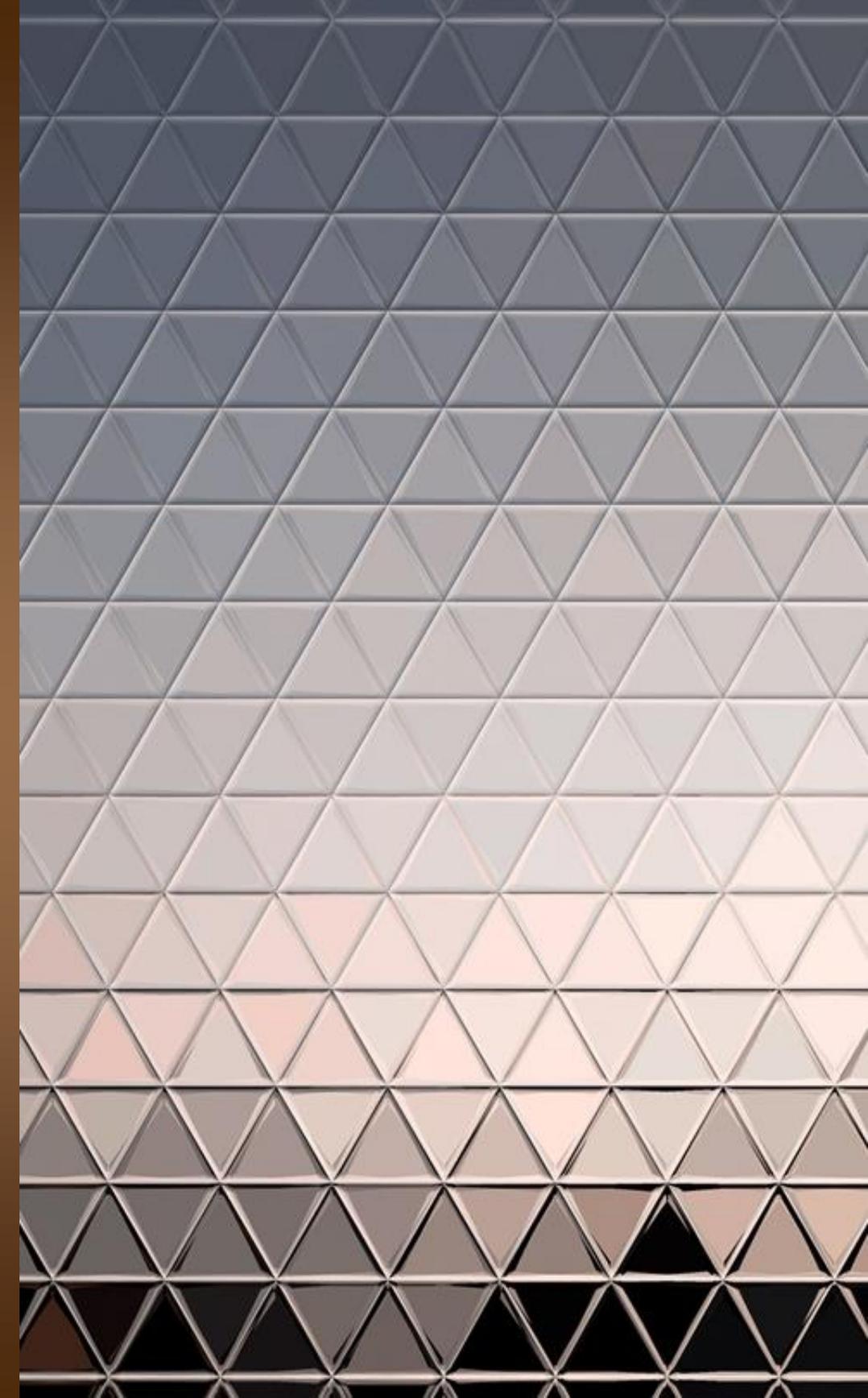


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Comparing Apples to Oranges:
Learning Similarity Functions for Data
Produced by Different Distributions

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Individual Fairness

- Introduced by Dwork et al. ([Fairness through Awareness, ITCS 2012](#))

Similar individuals should be treated similarly

- How can you define similarity between individuals?
 - i. For every two elements x, y you are given $\sigma(x, y) \in [0,1]$
 - ii. The smaller $\sigma(x, y)$ is the more similar the elements
- The similarity function is always assumed given

Main Obstacle and Prior Work

- Similarity scores are not trivial to obtain (even raised in Dwork et al.)
 - Deferred to third parties
 - Ideally should be learned
- C. Ilvento. ([Metric learning for individual fairness, FAccT 2019](#)) learns similarity scores through the use of oracle queries
 - **Assumption:** The $\sigma(x, y)$ form a metric space
- Mukherjee et al. ([Two simple ways to learn individual fairness metrics from data, ICML 2020](#))
 - Learns a specific metric function
- Wang et al. ([An empirical study on learning fairness metrics for compas data with human supervision, 2019](#))
 - Purely empirical and focuses on specific metrics

Our Setting

- **Starting point:** Learning similarities is sometimes easy and other times hard
 - **Easy:** Comparing homogeneous data; same “demographic” group (equivalently data produced by the same distribution)
 - **Hard:** Comparing heterogeneous data; different demographics
 - **E.g.:** PhD admissions. Comparisons for students from different universities are hard

- Feature space \mathcal{I} . γ “demographic” groups, where each $\ell \in [\gamma]$ is governed by a distribution \mathcal{D}_ℓ . $x \sim \mathcal{D}_\ell$ denotes an element $x \in \mathcal{I}$ that is randomly drawn from \mathcal{D}_ℓ . The support of each distribution corresponds to the members of the group.
- For each $\ell \in [\gamma]$ there exists a given **metric** similarity function $d_\ell: \mathcal{I}^2 \mapsto [0,1]$.
- For every distinct ℓ, ℓ' there exists an unknown similarity function $\sigma_{\ell, \ell'}: \mathcal{I}^2 \mapsto [0,1]$.

Computational Goal

Goal of Our Problem: We want for any two groups ℓ, ℓ' to compute a function $f_{\ell, \ell'} : \mathcal{I}^2 \mapsto \mathbb{R}_{\geq 0}$, such that $f_{\ell, \ell'}(x, y)$ is our estimate of similarity for any $x \in \mathcal{D}_\ell$ and $y \in \mathcal{D}_{\ell'}$. Specifically, we seek a PAC (Probably Approximately Correct) guarantee, where for any given accuracy and confidence parameters $\epsilon, \delta \in (0, 1)$ we have:

$$\Pr_{x \sim \mathcal{D}_\ell, y \sim \mathcal{D}_{\ell'}} \left[|f_{\ell, \ell'}(x, y) - \sigma_{\ell, \ell'}(x, y)| > \epsilon \right] \leq \delta$$

Tools for learning:

- i. For each ℓ a set S_ℓ of i.i.d. samples from \mathcal{D}_ℓ
- ii. Access to an expert oracle. You provide the oracle with $x \in \mathcal{D}_\ell$ and $y \in \mathcal{D}_{\ell'}$, and it returns $\sigma_{\ell, \ell'}(x, y)$

Objectives:

- i. Polynomial number of samples
- ii. Minimum queries

Results

- Algorithm with provable PAC guarantees:
 - i. Almost optimal error probability (no free lunch theorem)
 - ii. Almost optimal number of queries (lower bound on queries required)
 - iii. Experimental validation