

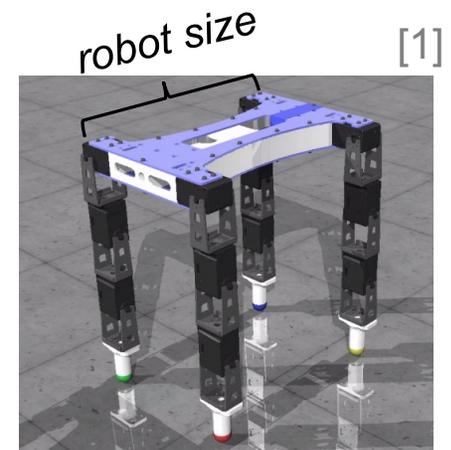
# Importance-aware Co-teaching for Offline Model-based Optimization

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# Problem Background

- Design objects with specific desired properties.
  - For example: Design a new robot to run faster.
- Evaluation can be expensive, so assume access only to an offline dataset of designs and their property scores.
  - For example: some pairs of robot size and running speed.
- **Offline Model-based Optimization (MBO)**: find a design (robot size) to maximize its property (speed) with the offline dataset only.



# Problem Formulation

$$\arg \max_{\mathcal{A}} [\mathbb{P}(\{f(\mathbf{x}^*) : \mathbf{x}^* \in \mathcal{A}(\mathcal{D}, K)\}, n)].$$

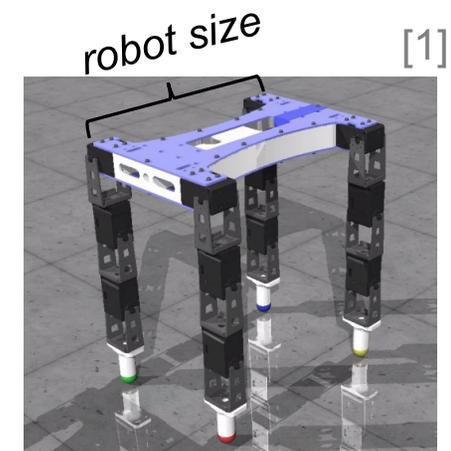
$\mathbf{x}_i$  : some design (robot size);

$y_i = f(\mathbf{x}_i)$  : some property (robot speed);

$\mathcal{D} = \{(\mathbf{x}_i, y_i)\}_{i=1}^N$  : an offline dataset;

$\mathcal{A}$  : some algorithm outputs  $K$  candidates

$\mathbb{P}(S, n)$  : the  $n^{\text{th}}$  percentile of  $S$ .



## Related Work

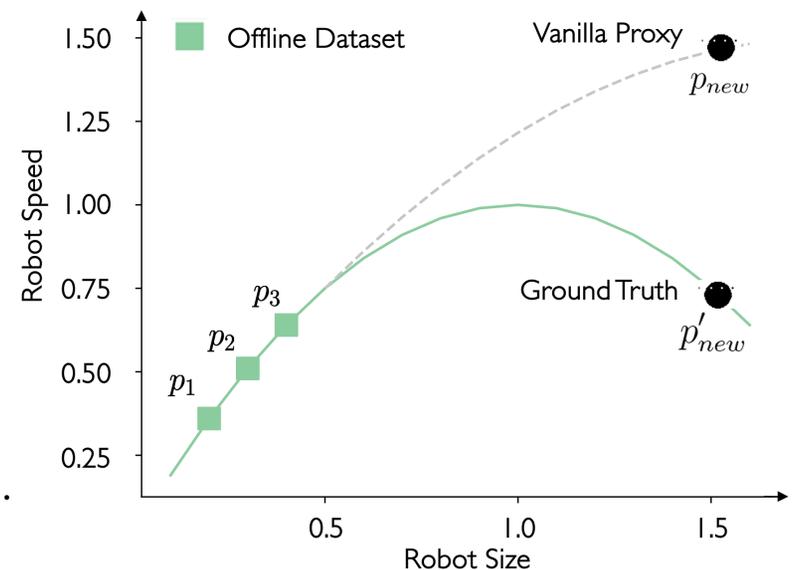
A common approach consists of 2 steps:

- 1) Fit a DNN proxy  $f_{\theta}(\cdot)$  to  $\mathcal{D}$ .

$$\theta^* = \arg \min_{\theta} \frac{1}{N} \sum_{i=1}^N (f_{\theta}(\mathbf{x}_i) - y_i)^2.$$

- 2) Perform gradient ascent:

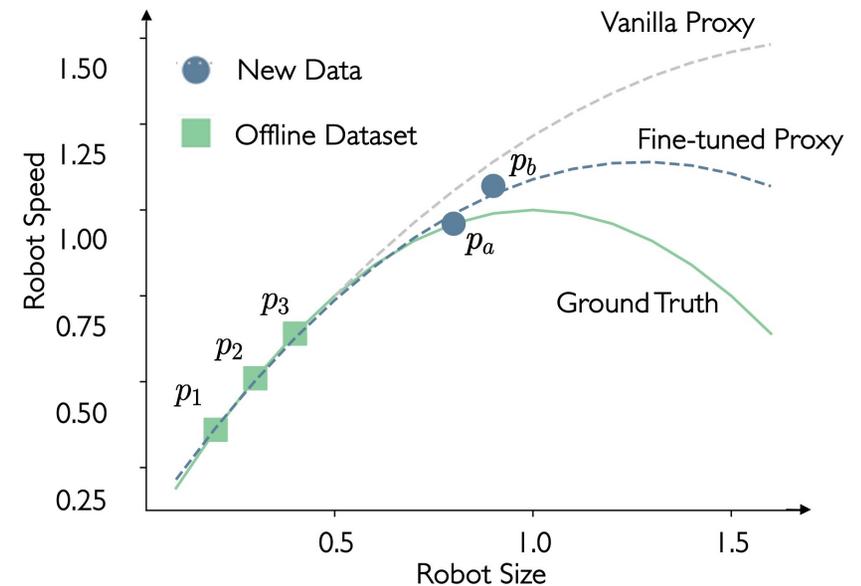
$$\mathbf{x}_t = \mathbf{x}_{t-1} + \eta \nabla_{\mathbf{x}} f_{\theta}(\mathbf{x}) \Big|_{\mathbf{x}=\mathbf{x}_t}, \quad \text{for } t \in [1, T].$$



**Out-of-distribution (OOD) issue:** The proxy overestimates the ground truth objective function, and the seemingly high-scoring design  $p_{new}$  obtained by gradient ascent has a low ground truth score.

# Motivation

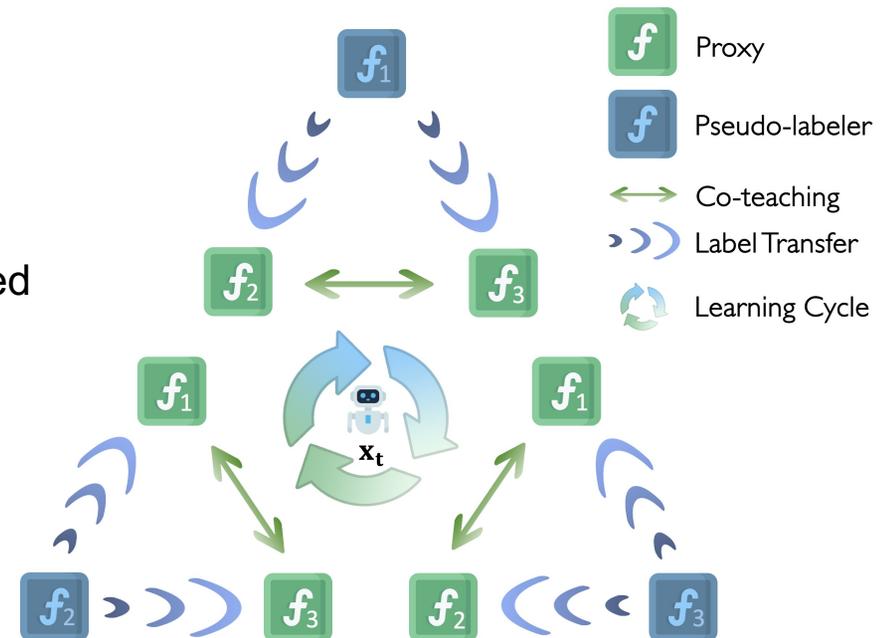
- What if we have more data points?
  - May train a better proxy!
- How to obtain these new data points?
  - Sample a set of points and use one proxy to pseudo-label them.
- How to identify the more accurate data points?
  - Let another two proxies co-teach each other to exchange valuable data.





## Methodology: Pseudo-label-driven Co-teaching

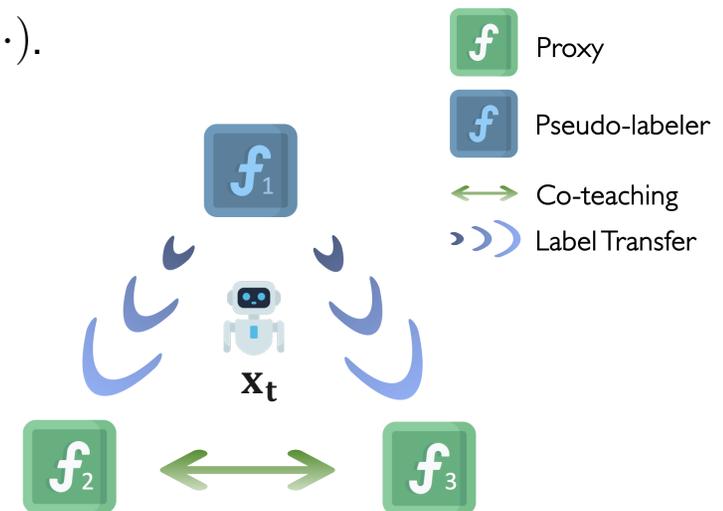
- Maintain three symmetric proxies and use their mean ensemble as the final proxy.
- Select one proxy as the pseudo-labeler, followed by a co-teaching process to enable knowledge sharing between the other two proxies.
- Repeat this process three times with different proxies as the pseudo-labeler in turn.





## Methodology: Pseudo-label-driven Co-teaching

- Maintain three symmetric proxies,  $f_{\theta_1}(\cdot)$ ,  $f_{\theta_2}(\cdot)$ , and  $f_{\theta_3}(\cdot)$ .
- Generate a set of points near the current point  $x_t$  and use  $f_{\theta_1}(\cdot)$  to pseudo-label it.
- $f_{\theta_2}(\cdot)$  and  $f_{\theta_3}(\cdot)$  co-teach each other by exchanging the small-loss samples in the pseudo-labeled dataset.

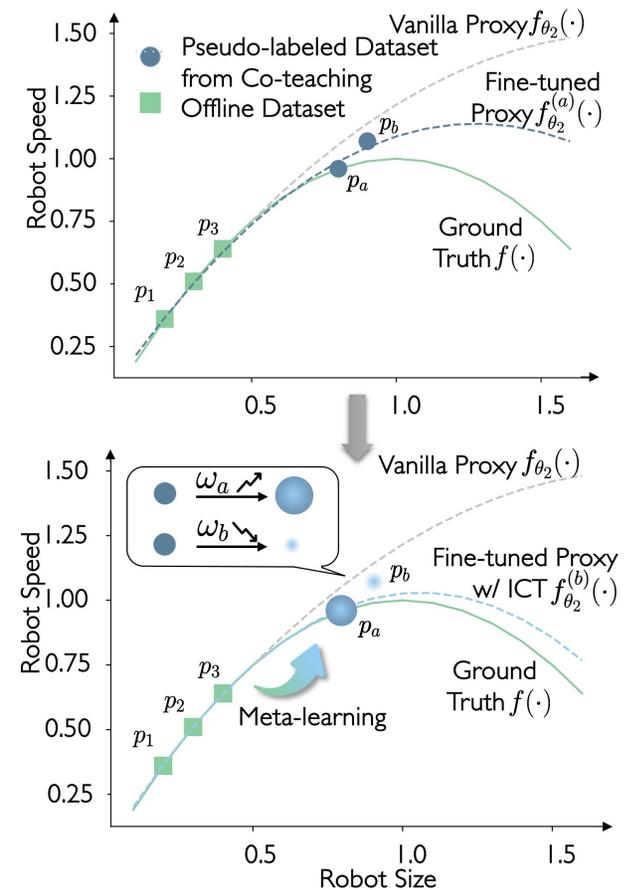


# Methodology: Meta-learning-based Sample Reweighting

- Assign an importance weight  $\omega_i$  to the  $i^{th}$  selected sample.
- Leverage the supervision signals from the offline dataset to update the weight:

$$\begin{aligned} \omega'_i &= \omega_i - \beta \frac{\partial \mathcal{L}(\theta^*(\omega))}{\partial \theta} \frac{\partial \theta^*(\omega)}{\partial \omega_i} \\ &= \omega_i + \frac{\alpha \beta}{K} \frac{\partial \mathcal{L}(\theta^*(\omega))}{\partial \theta} \frac{\partial (f_{\theta}(\mathbf{x}_i^s) - \bar{y}_i^s)^2}{\partial \theta^\top}, \end{aligned}$$

where  $\mathcal{L}(\theta^*(\omega)) = \arg \min_{\omega} \frac{1}{N} \sum_{i=1}^N (f_{\theta^*(\omega)}(\mathbf{x}_i) - y_i)^2$  is the loss on the offline data set.





# Experimental Results: Continuous Tasks

Table 1: Experimental results on continuous tasks for comparison.

Method	Superconductor	Ant Morphology	D’Kitty Morphology	Hopper Controller
$\mathcal{D}(\text{best})$	0.399	0.565	0.884	1.0
BO-qEI	$0.402 \pm 0.034$	$0.819 \pm 0.000$	$0.896 \pm 0.000$	$0.550 \pm 0.018$
CMA-ES	$0.465 \pm 0.024$	<b><math>1.214 \pm 0.732</math></b>	$0.724 \pm 0.001$	$0.604 \pm 0.215$
REINFORCE	$0.481 \pm 0.013$	$0.266 \pm 0.032$	$0.562 \pm 0.196$	$-0.020 \pm 0.067$
CbAS	<b><math>0.503 \pm 0.069</math></b>	$0.876 \pm 0.031$	$0.892 \pm 0.008$	$0.141 \pm 0.012$
Auto.CbAS	$0.421 \pm 0.045$	$0.882 \pm 0.045$	$0.906 \pm 0.006$	$0.137 \pm 0.005$
MIN	$0.499 \pm 0.017$	$0.445 \pm 0.080$	$0.892 \pm 0.011$	$0.424 \pm 0.166$
Grad	$0.483 \pm 0.025$	$0.920 \pm 0.044$	<b><math>0.954 \pm 0.010</math></b>	<b><math>1.791 \pm 0.182</math></b>
Mean	$0.497 \pm 0.011$	$0.943 \pm 0.012$	<b><math>0.961 \pm 0.012</math></b>	<b><math>1.815 \pm 0.111</math></b>
Min	<b><math>0.505 \pm 0.017</math></b>	$0.910 \pm 0.038$	$0.936 \pm 0.006$	$0.543 \pm 0.010$
COMs	$0.472 \pm 0.024$	$0.828 \pm 0.034$	$0.913 \pm 0.023$	$0.658 \pm 0.217$
ROMA	<b><math>0.510 \pm 0.015</math></b>	$0.917 \pm 0.030$	$0.927 \pm 0.013$	$1.740 \pm 0.188$
NEMO	$0.502 \pm 0.002$	$0.952 \pm 0.002$	<b><math>0.950 \pm 0.001</math></b>	$0.483 \pm 0.005$
BDI	<b><math>0.513 \pm 0.000</math></b>	$0.906 \pm 0.000$	$0.919 \pm 0.000$	<b><math>1.993 \pm 0.000</math></b>
IOM	<b><math>0.520 \pm 0.018</math></b>	$0.918 \pm 0.031$	$0.945 \pm 0.012$	$1.176 \pm 0.452$
<b>ICT<sub>(ours)</sub></b>	<b><math>0.503 \pm 0.017</math></b>	<b><math>0.961 \pm 0.007</math></b>	<b><math>0.968 \pm 0.020</math></b>	<b><math>2.104 \pm 0.357</math></b>

**Our method achieves top performance on all four continuous tasks.**



# Experimental Results: Discrete Tasks and Rankings

Table 2: Experimental results on discrete tasks, and ranking on all tasks for comparison.

Method	TF Bind 8	TF Bind 10	NAS	Rank Mean	Rank Median
$\mathcal{D}(\mathbf{best})$	0.439	0.467	0.436		
BO-qEI	$0.798 \pm 0.083$	$0.652 \pm 0.038$	<b><math>1.079 \pm 0.059</math></b>	9.9/15	11/15
CMA-ES	<b><math>0.953 \pm 0.022</math></b>	$0.670 \pm 0.023$	$0.985 \pm 0.079$	6.1/15	3/15
REINFORCE	<b><math>0.948 \pm 0.028</math></b>	$0.663 \pm 0.034$	$-1.895 \pm 0.000$	11.3/15	15/15
CbAS	$0.927 \pm 0.051$	$0.651 \pm 0.060$	$0.683 \pm 0.079$	9.1/15	9/15
Auto.CbAS	$0.910 \pm 0.044$	$0.630 \pm 0.045$	$0.506 \pm 0.074$	11.6/15	12/15
MIN	$0.905 \pm 0.052$	$0.616 \pm 0.021$	$0.717 \pm 0.046$	11.0/15	12/15
Grad	$0.906 \pm 0.024$	$0.635 \pm 0.022$	$0.598 \pm 0.034$	7.7/15	9/15
Mean	$0.899 \pm 0.025$	$0.652 \pm 0.020$	$0.666 \pm 0.062$	6.6/15	6/15
Min	$0.939 \pm 0.013$	$0.638 \pm 0.029$	$0.705 \pm 0.011$	7.3/15	8/15
COMs	$0.452 \pm 0.040$	$0.624 \pm 0.008$	$0.810 \pm 0.029$	10.3/15	12/15
ROMA	$0.924 \pm 0.040$	$0.666 \pm 0.035$	$0.941 \pm 0.020$	5.1/15	5/15
NEMO	$0.941 \pm 0.000$	<b><math>0.705 \pm 0.000</math></b>	$0.734 \pm 0.015$	5.0/15	4/15
BDI	$0.870 \pm 0.000$	$0.605 \pm 0.000$	$0.722 \pm 0.000$	7.9/15	8/15
IOM	$0.878 \pm 0.069$	$0.648 \pm 0.023$	$0.274 \pm 0.021$	7.6/15	6/15
<b>ICT<sub>(ours)</sub></b>	<b><math>0.958 \pm 0.008</math></b>	<b><math>0.691 \pm 0.023</math></b>	$0.667 \pm 0.091$	<b>3.1/15</b>	<b>2/15</b>

**Our method achieves top performance on 2/3 discrete tasks.**



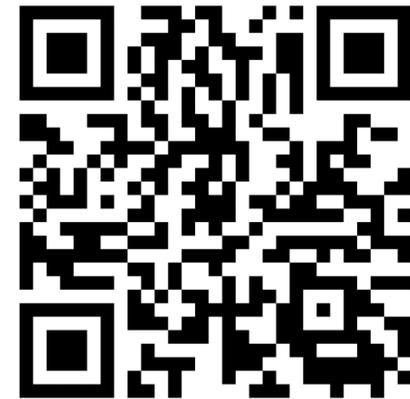
# Thanks for your attention!



Paper



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