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LD²: Scalable Heterophilous GNN with Decoupled Embeddings

Ningyi Liao

Siqiang Luo

Xiang Li

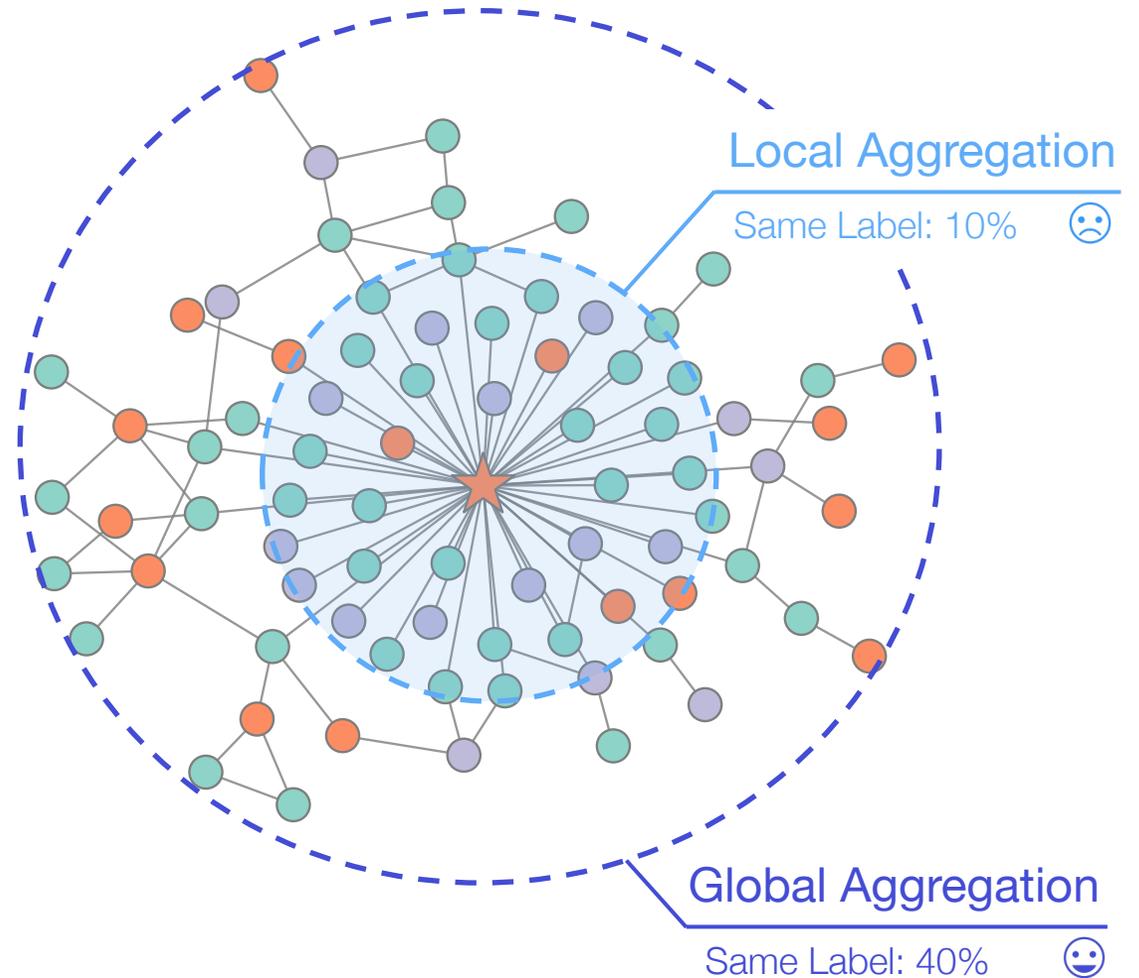
Jieming Shi

PRESENT BY: Ningyi Liao



Background: Heterophilous GNN

- Heterophily: connected nodes tend to be of dissimilar labels
- Example: fraudster – normal user in transaction networks
- **Locality**-based GNNs not suitable under heterophily
- Existing heterophilous GNNs rely on **global computation**



Challenge: Hetero GNNs not Scalable Enough

Natural conflict:

Global Computation vs Scalability & Minibatch

Model	Time - Precomp	Time - Train	Time - Test	GPU Memory
GPRGNN	$O(m)$	$O(IL_P mF + ILnF^2)$	$O(L_P mF + LnF^2)$	$O(LnF + m + LF^2)$
GCNJK	–	$O(ILmF + ILnF^2)$	$O(LmF + LnF^2)$	$O(L_C nF + L_C F^2)$
MixHop	–	$O(IL_P LmF + ILnF^2)$	$O(L_P LmF + LnF^2)$	$O(CLnF + CLF^2)$
LINKX	–	$O(ImF + ILnF^2)$	$O(mF + LnF^2)$	$O(L_C n_b F + L_C F^2 + nF)$
LD ² (ours)	$O(L_P mF)$	$O(ILnF^2)$	$O(LnF^2)$	$O(L_C n_b F + L_C F^2)$



Terms that not scalable to large m and n



Terms that not suitable for minibatch

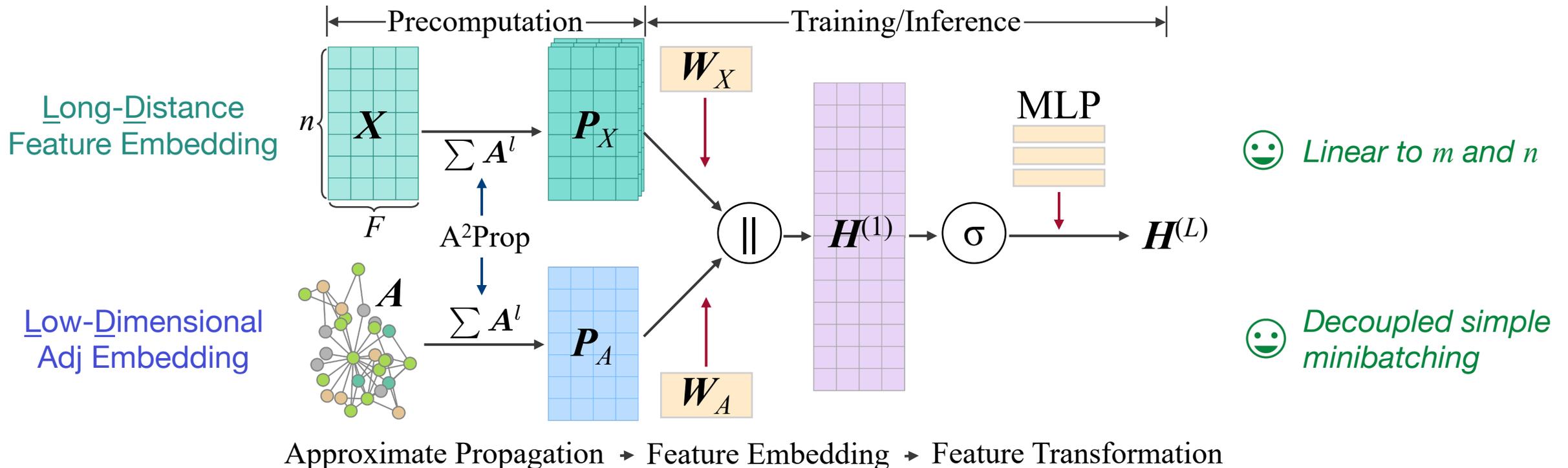
Method: LD² Framework

- Precomputation:

$$P_A, P_X = A^2\text{Prop}(A, X)$$

- Feature Transformation:

$$H^{(L)} = \text{MLP}(P_A W_A \| P_X W_X)$$



Method: Adjacency Embedding

- Low-Dimensional 2-hop adjacency decomposition

$$P_A \cdot P_A^T \approx A^2$$

Adj Embedding
Dense $n \times F$

2-hop Adj Matrix
Sparse $n \times n$

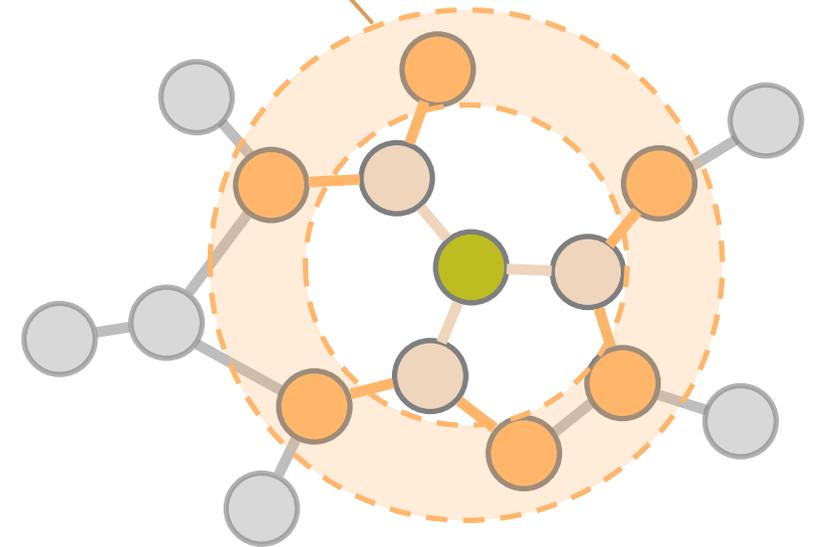
- Calculation:

$$P_A = \phi(A^2 \cdots \phi(A^2 \mathcal{N}))$$

Orthonormalize

Gaussian Matrix

2-hop Neighborhood

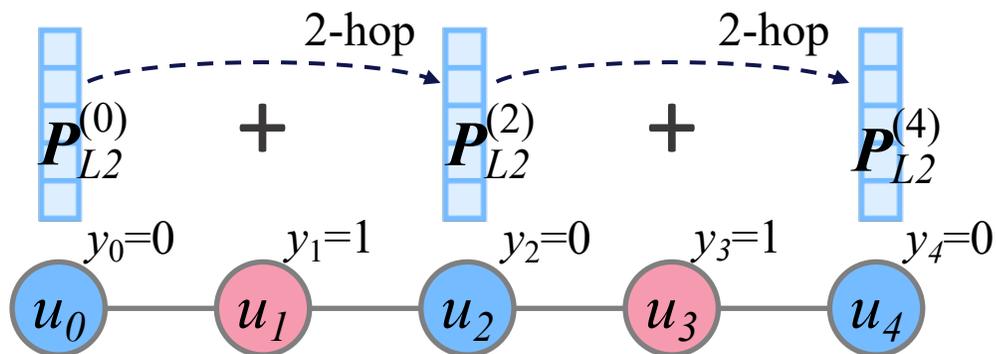


Method: Feature Embedding

- Long-Distance generalized graph propagation

CHANNEL①: *Constant* 2-hop
Adjacency Propagation

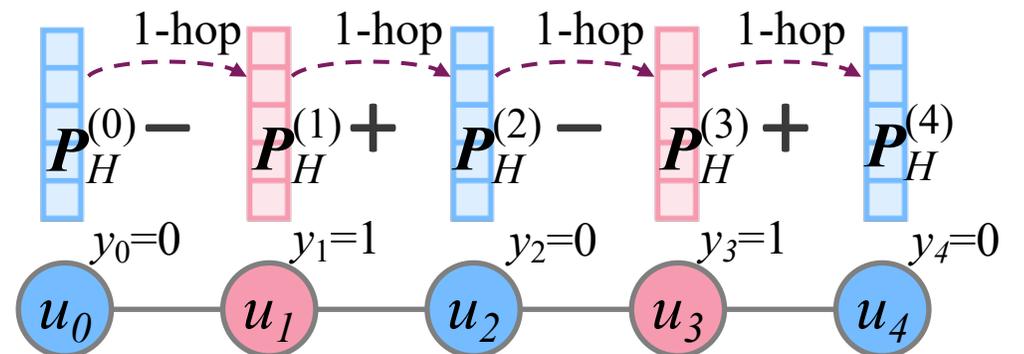
$$P_{X,L2} = \sum_{l=1}^L \bar{A}^{2l} \cdot X$$



CHANNEL②: *Inverse* 1-hop
Laplacian Propagation

$$P_{X,H} = \sum_{l=1}^L (\tilde{L} + I)^l \cdot X$$

Laplacian $\tilde{L} = I - \tilde{A}$



Evaluation: Effectiveness

- Top 1 accuracy on 6/8 large-scale heterophilous datasets
- No accuracy drop for minibatch

Dataset	genius	tolokers	arxiv-year	penn94	twitch-gamers	pokec	snap-patents	wiki
Nodes n	421,858	11,758	169,343	41,536	168,114	1,632,803	2,738,035	1,770,981
Edges m	922,864	1,038,000	1,157,799	1,362,220	6,797,557	22,301,964	13,967,949	242,507,069
F / N_c	12 / 2	10 / 2	128 / 5	4,814 / 2	7 / 2	65 / 2	269 / 5	600 / 5
MLP	82.47 \pm 0.06	73.38 \pm 0.25	37.23 \pm 0.31	74.41 \pm 0.48	61.26 \pm 0.19	61.81 \pm 0.07	23.03 \pm 1.48	35.64 \pm 0.10
PPRGo	79.81 \pm 0.00	<u>78.16</u> \pm 0.00	39.35 \pm 0.12	58.75 \pm 0.31	47.19 \pm 2.26	50.61 \pm 0.04	(>12h)	(>12h)
SGC	79.85 \pm 0.01	71.16 \pm 0.06	43.40 \pm 0.16	68.31 \pm 0.27	57.05 \pm 0.21	56.58 \pm 0.06	37.70 \pm 0.06	28.12 \pm 0.08
GCNJK-GS	80.65 \pm 0.07	74.41 \pm 0.73	48.26 \pm 0.64	65.91 \pm 0.16	59.91 \pm 0.42	59.38 \pm 0.21	33.64 \pm 0.05	42.95 \pm 0.39
MixHop-GS	80.63 \pm 0.04	77.47 \pm 0.40	49.26 \pm 0.16	75.00 \pm 0.37	61.80 \pm 0.00	64.02 \pm 0.02	34.73 \pm 0.15	45.52 \pm 0.11
LINKX	82.51 \pm 0.10	77.74 \pm 0.13	50.44 \pm 0.30	78.63 \pm 0.25	64.15 \pm 0.18	68.64 \pm 0.65	52.69 \pm 0.05	50.59 \pm 0.12
LD² (ours)	85.31 \pm 0.06	79.76 \pm 0.26	<u>50.29</u> \pm 0.11	75.52 \pm 0.10	64.33 \pm 0.19	74.93 \pm 0.10	58.58 \pm 0.34	52.91 \pm 0.16

Evaluation: Efficiency

- 3-15× faster minibatch training, significantly fast inference
- Up to 5× lower GPU memory for large graphs

Dataset	twitch-gamers			pokec			snap-patents			wiki		
	Learn	Infer	Mem.	Learn	Infer	Mem.	Learn	Infer	Mem.	Learn	Infer	Mem.
MLP	6.36	0.02	0.61	47.86	0.11	13.77	27.39	0.28	9.33	133.55	0.62	18.15
PPRGo	10.46+15.88	0.41	9.64	121.95+56.11	2.69	3.82	(>12h)			(>12h)		
SGC	0.09+0.74	0.01	0.28	1.05+8.08	0.01	0.28	4.94+23.54	0.01	0.42	12.66+7.98	0.01	0.52
GCNJK-GS	71.48	0.02*	7.33	<u>27.33</u>	0.09*	<u>9.03</u>	<u>19.02</u>	0.23*	<u>9.21</u>	95.52	0.69*	16.36
MixHop-GS	52.12	<u>0.01*</u>	<u>1.49</u>	71.35	<u>0.03*</u>	12.91	45.24	<u>0.16*</u>	19.58	<u>84.22</u>	<u>0.23*</u>	16.28
LINKX	10.99	0.19	2.35	28.77	0.33	9.03	39.80	0.22	21.53	180.71	1.14	14.53
LD² (ours)	0.85+ 1.96	0.01	1.44	17.95+ 6.18	0.01	3.82	31.32+ 6.96	0.02	3.96	28.12+ 6.50	0.01	4.47

THANK YOU

Acknowledgments

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