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Efficient Potential-based Exploration in Reinforcement Learning using Inverse Dynamic Bisimulation Metric

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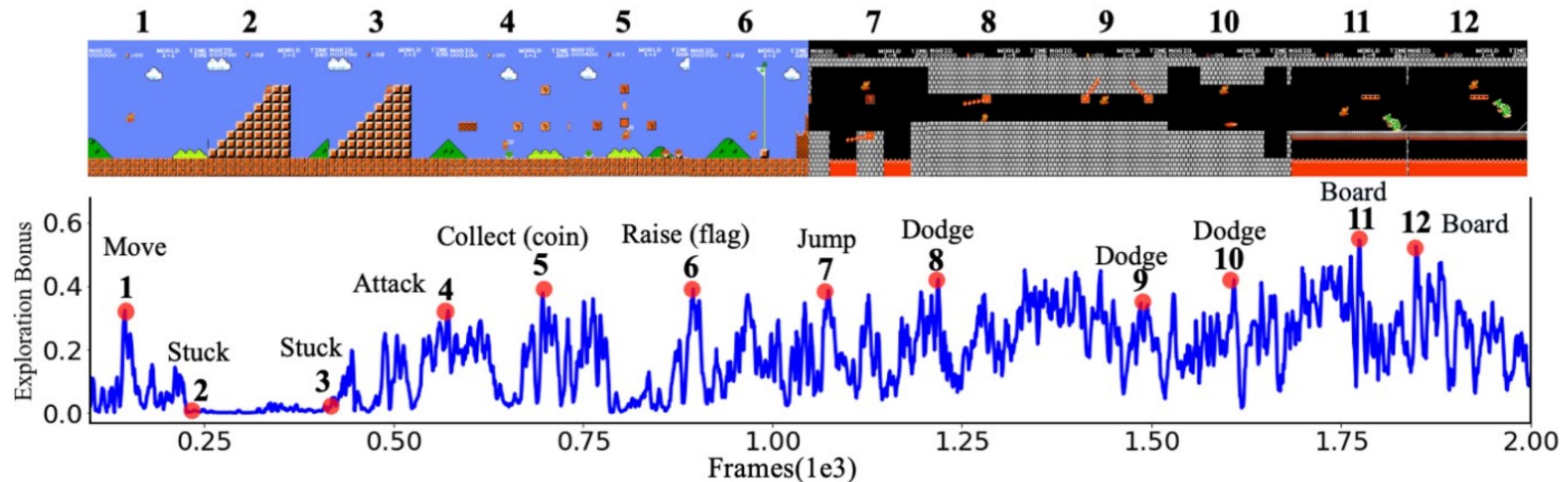
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Introduction to exploration in RL

- Reward shaping methods
 - Rely on human prior knowledge
 - Introduce human cognitive biases
- Curiosity-driven exploration methods
 - Lack of scalability
 - Rely on count-based episodic term
 - Cause policy variance of original MDP
- **LIBERTY: expLoration vIa Bisimulation mEtRic-based sTate discrepancY**
 - Our method (LIBERTY) uses the bisimulation metric to measure state discrepancy and propose a potential function based on the inverse dynamic bisimulation metric, which promotes effective exploration while preserving the optimal policy of the original MDP

Motivation: state discrepancy as exploration bonus

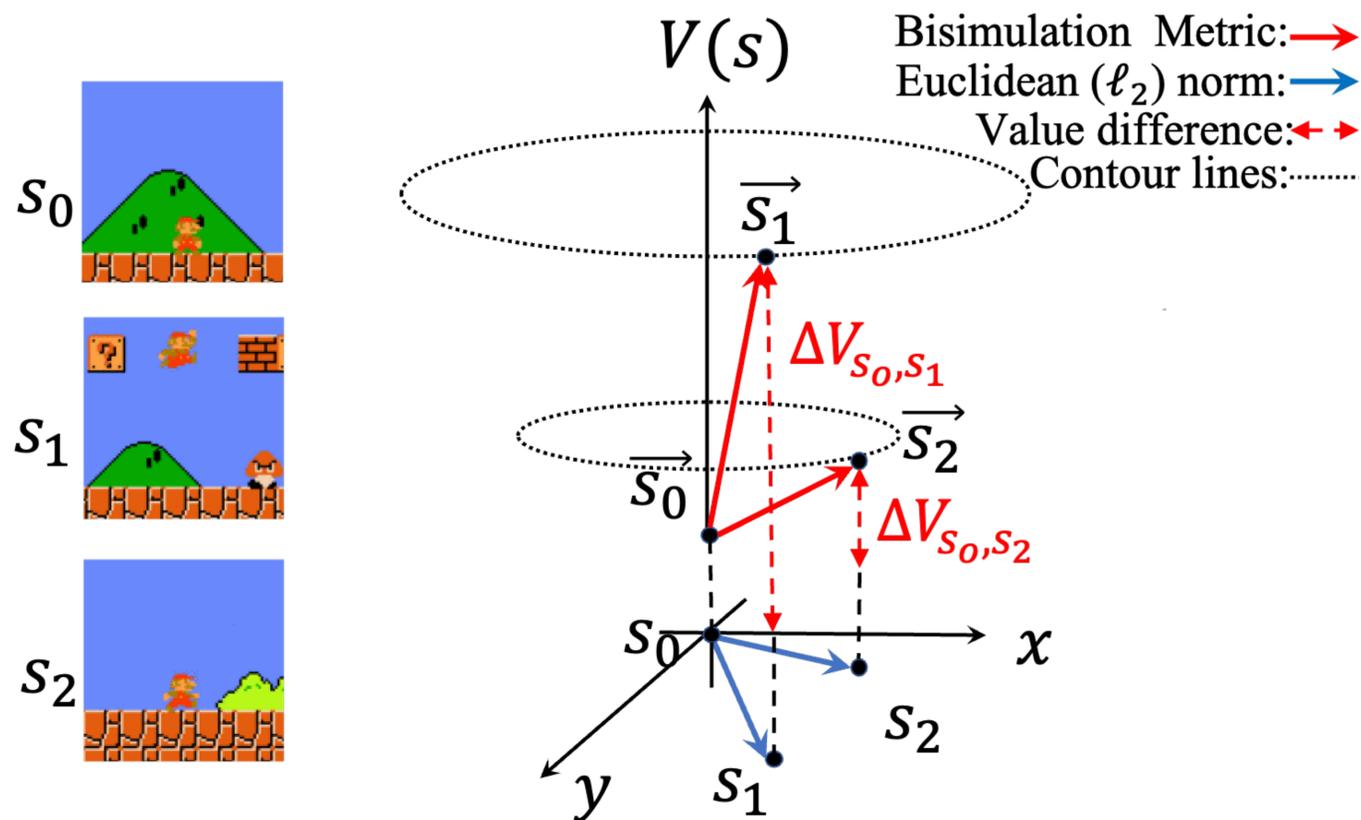


- Using the difference between states $d(s_i, s_j)$ as exploration bonus
- Many spikes are related to significant occurrences, e.g., moving forward (1), attacking enemies (4), collecting coins (5) etc. The reward is close to 0 when the agent is stuck (2,3)

Method: bisimulation metric measuring state discrepancy

- Bisimulation metric:

$$d_{\pi}(s_i, s_j) = |r_i^{\pi} - r_j^{\pi}| + \gamma W_1(d_{\pi}) \left(\mathcal{P}^{\pi}(\cdot | s_i), \mathcal{P}^{\pi}(\cdot | s_j) \right)$$



- Project the state into 3D latent space and Z axis denotes value
- Bisimulation metric identifies the **value differences** between states, enabling the agent to reach state s_1 with a higher value compared to s_2 , starting from initial state s_0

Method: inverse dynamic bisimulation metric

- **Meaningless exploration**: state difference is caused by background changing without taking actions



- Add inverse dynamic module ($I: S \times S \rightarrow A$) to avoid meaningless exploration

$$d_{inv}(s_i, s_j) = |r_i^\pi - r_j^\pi| + \gamma W_2(d_{inv}) \left(\mathcal{P}^\pi(\cdot | s_i), \mathcal{P}^\pi(\cdot | s_j) \right) \\ + \gamma \|I(\cdot | s_i, s_{i+1}) - I(\cdot | s_j, s_{j+1})\|_1$$

Method: inverse dynamic bisimulation metric (cont.)

- Potential function based on d_{inv}

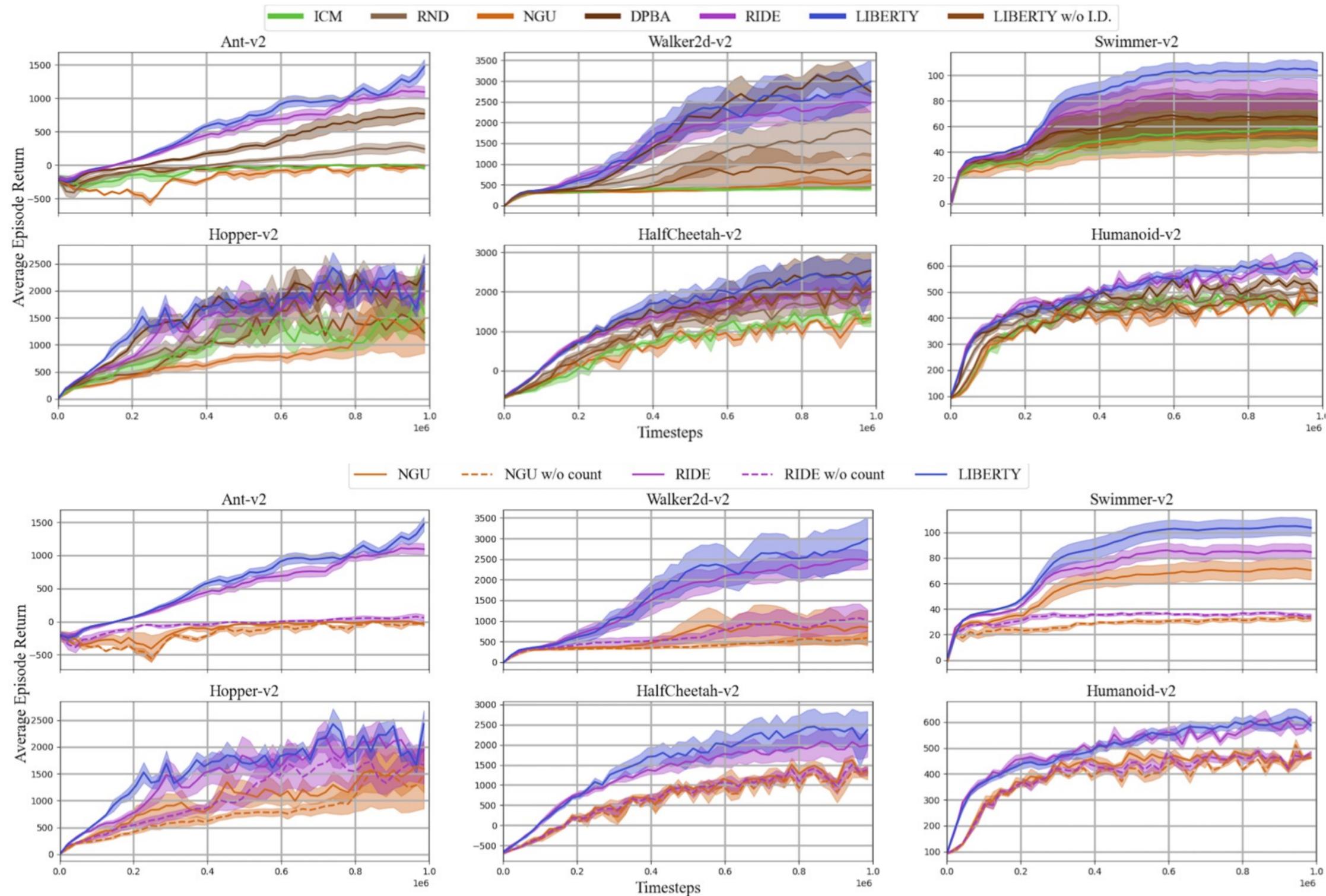
$$\Phi(s) = d_{inv}(s, s_0)$$

- Potential-based shaping reward function:

$$\mathcal{F}(s_t, a, s_{t+1}) = \gamma d_{inv}(s_{t+1}, s_0) - d_{inv}(s_t, s_0)$$

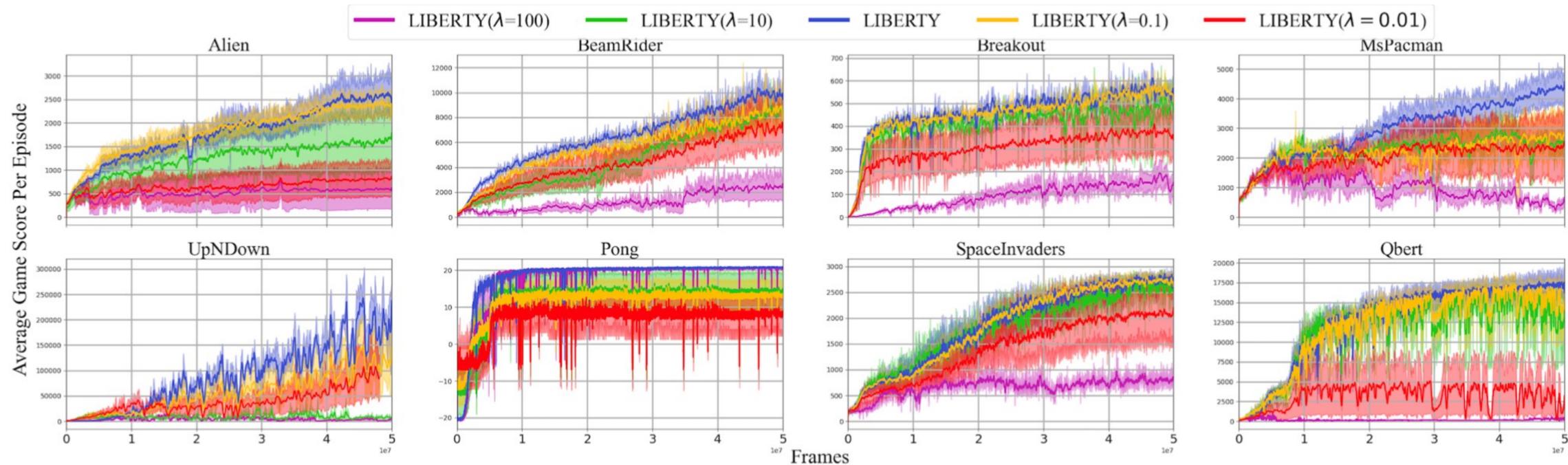
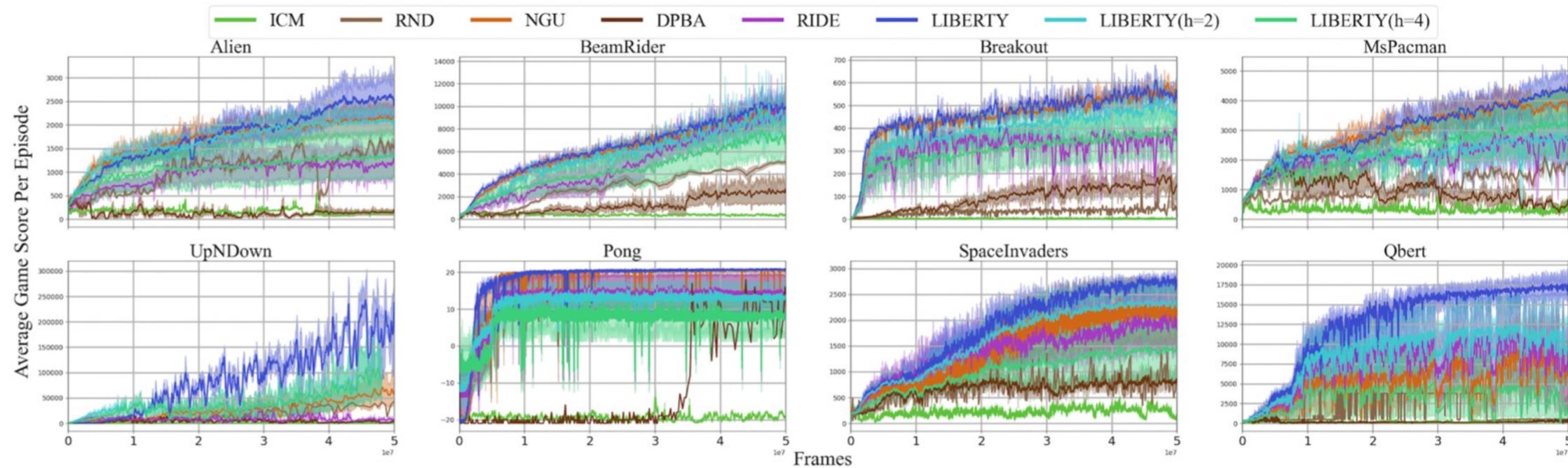
Experiment

- Results on MuJoCo continuous control



Experiment

- Results on Atari games with discrete actions



Experiment

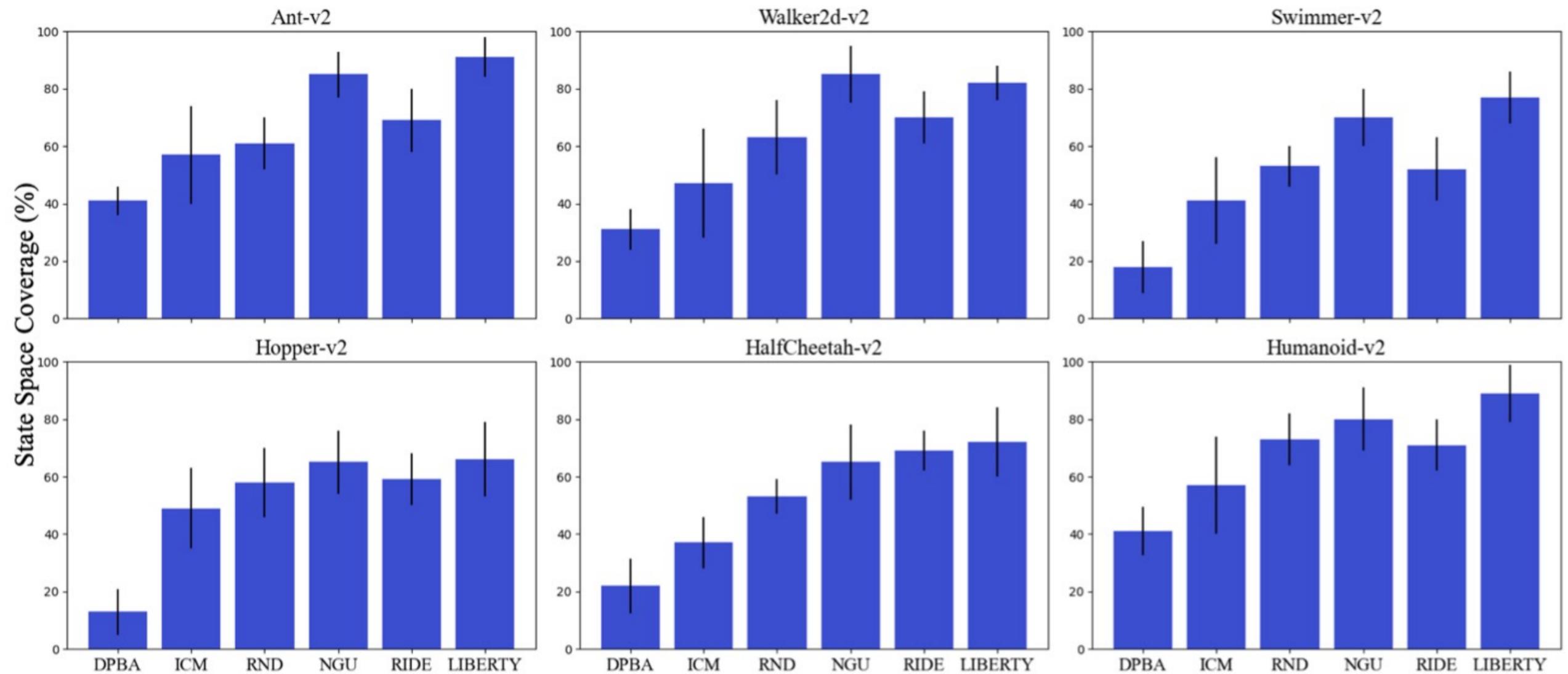
- Results on the delayed reward setting

Table 1: Quantitative results comparison between LIBERTY and other baseline methods in different environments of Mujoco with the delayed reward setting. The best and the runner-up results are (**bold**) and (underline)

Methods	Delay = 10					
	HalfCheetah	Hopper	Walker2d	Ant	Humanoid	Swimmer
ICM	1374 ± 368	1258 ± 325	1127 ± 225	-105 ± 43	462 ± 54	27 ± 11
RND	1694 ± 495	1976 ± 458	1405 ± 262	143 ± 17	532 ± 29	32 ± 15
NGU	1180 ± 513	989 ± 262	1275 ± 480	-164 ± 35	413 ± 78	24 ± 12
RIDE	<u>2467 ± 456</u>	1876 ± 431	1651 ± 325	92 ± 31	<u>570 ± 45</u>	<u>65 ± 16</u>
DPBA	<u>1514 ± 365</u>	<u>2103 ± 129</u>	<u>1997 ± 115</u>	592 ± 67	518 ± 23	43 ± 17
LIBERTY	2973 ± 437	2479 ± 315	2766 ± 487	<u>292 ± 68</u>	681 ± 73	73 ± 21
LIBERTY w/o I.D.	1783 ± 412	1676 ± 275	1732 ± 392	131 ± 22	505 ± 37	46 ± 11
Methods	Delay = 40					
	HalfCheetah	Hopper	Walker2d	Ant	Humanoid	Swimmer
ICM	919 ± 199	857 ± 175	697 ± 172	-213 ± 27	403 ± 34	13 ± 7
RND	1276 ± 387	1683 ± 338	968 ± 168	71 ± 15	<u>483 ± 25</u>	17 ± 11
NGU	1028 ± 405	879 ± 155	997 ± 280	-198 ± 27	387 ± 27	11 ± 6
RIDE	<u>1798 ± 355</u>	1235 ± 269	<u>1025 ± 282</u>	63 ± 18	468 ± 23	32 ± 11
DPBA	<u>883 ± 275</u>	1382 ± 85	<u>1016 ± 129</u>	<u>105 ± 31</u>	405 ± 15	9 ± 3
LIBERTY	2039 ± 315	<u>1612 ± 215</u>	1921 ± 372	142 ± 45	566 ± 35	<u>31 ± 13</u>
LIBERTY w/o I.D.	1231 ± 253	<u>1213 ± 207</u>	1012 ± 358	58 ± 13	455 ± 27	<u>17 ± 8</u>

Experiment

- Results on the reward-free setting



Contribution

- We develop a new potential function to ensure policy invariance without the need for **prior human knowledge**
- Our approach achieves **more efficient** exploration by encouraging agents to explore states with higher TD-error
 - Theorem 1(value difference bound):
$$|V^\pi(s_i) - V^\pi(s_j)| \leq d_{inv}(s_i, s_j)$$
 - Theorem 2(approximation of optimal value function):
$$d_{inv}(s, s_0) \approx V^*(s)$$
- Our method achieves best performance across various settings in extensive environments, which demonstrate its **scalability** and **superiority** compared with other methods

Thank you for your attention!



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Code is available